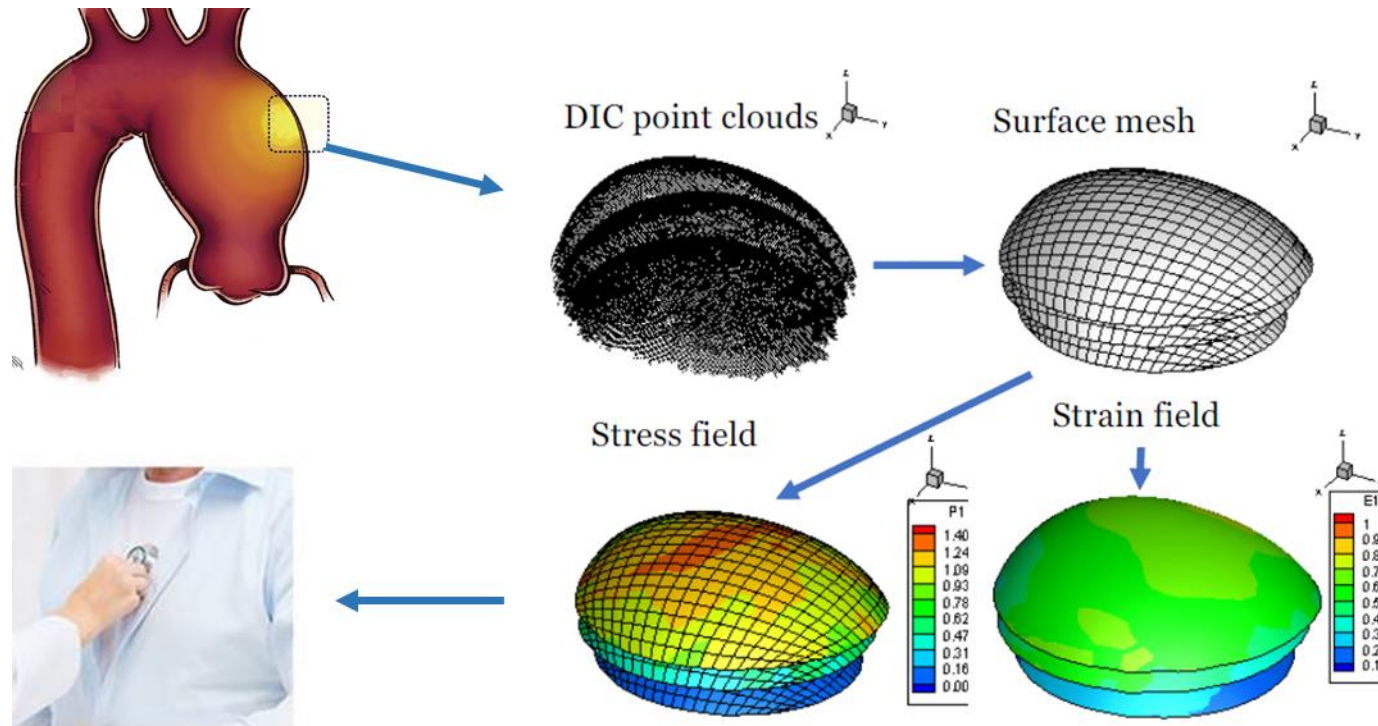


# 719.001 - Mechanics of biological tissues (2 SSt VO, WS 2021-2022)

Lecturers:

Prof Stéphane Avril, [Mines Saint-Etienne](#) (France)

Prof Gerhard Holzapfel, TU Graz

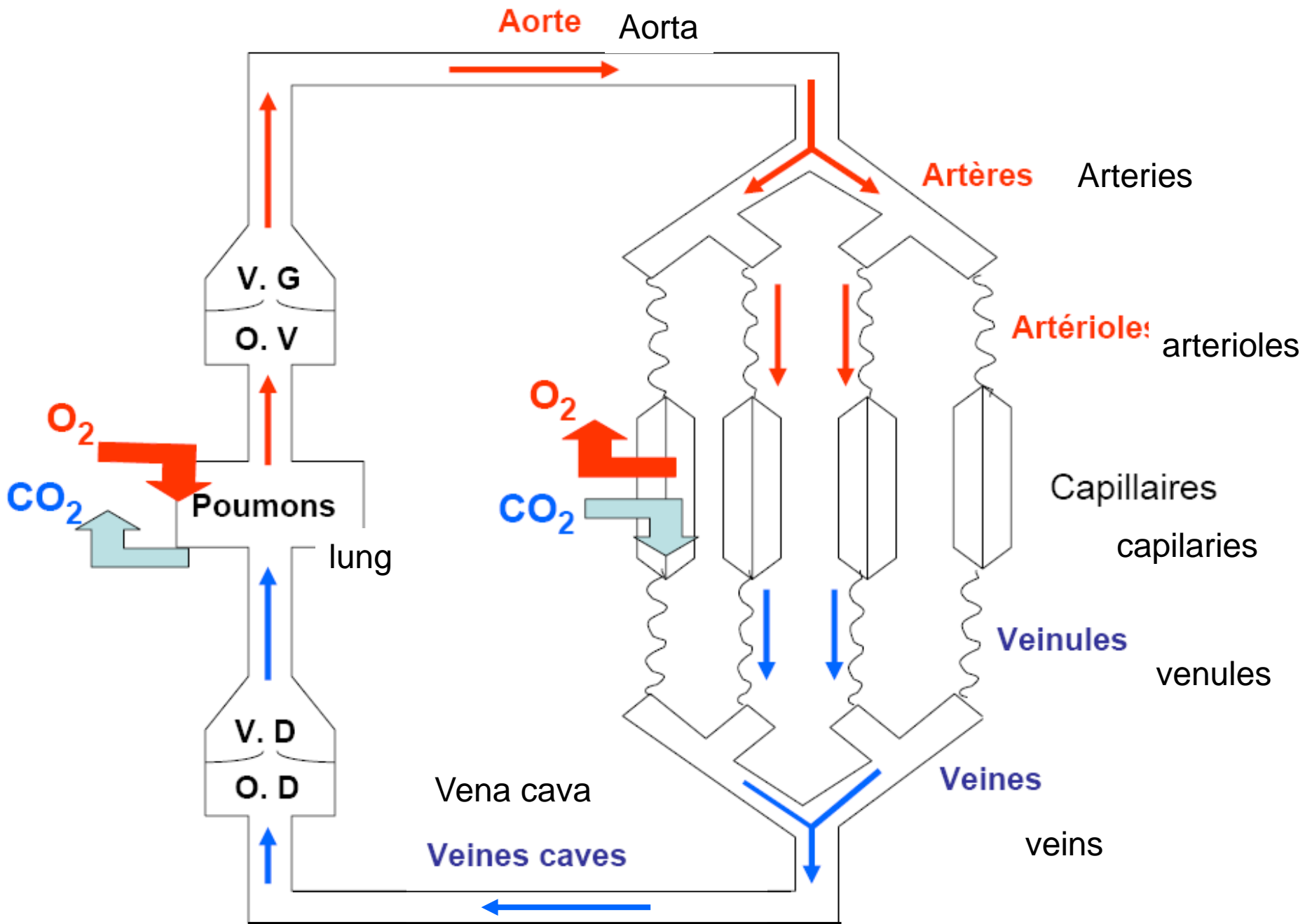


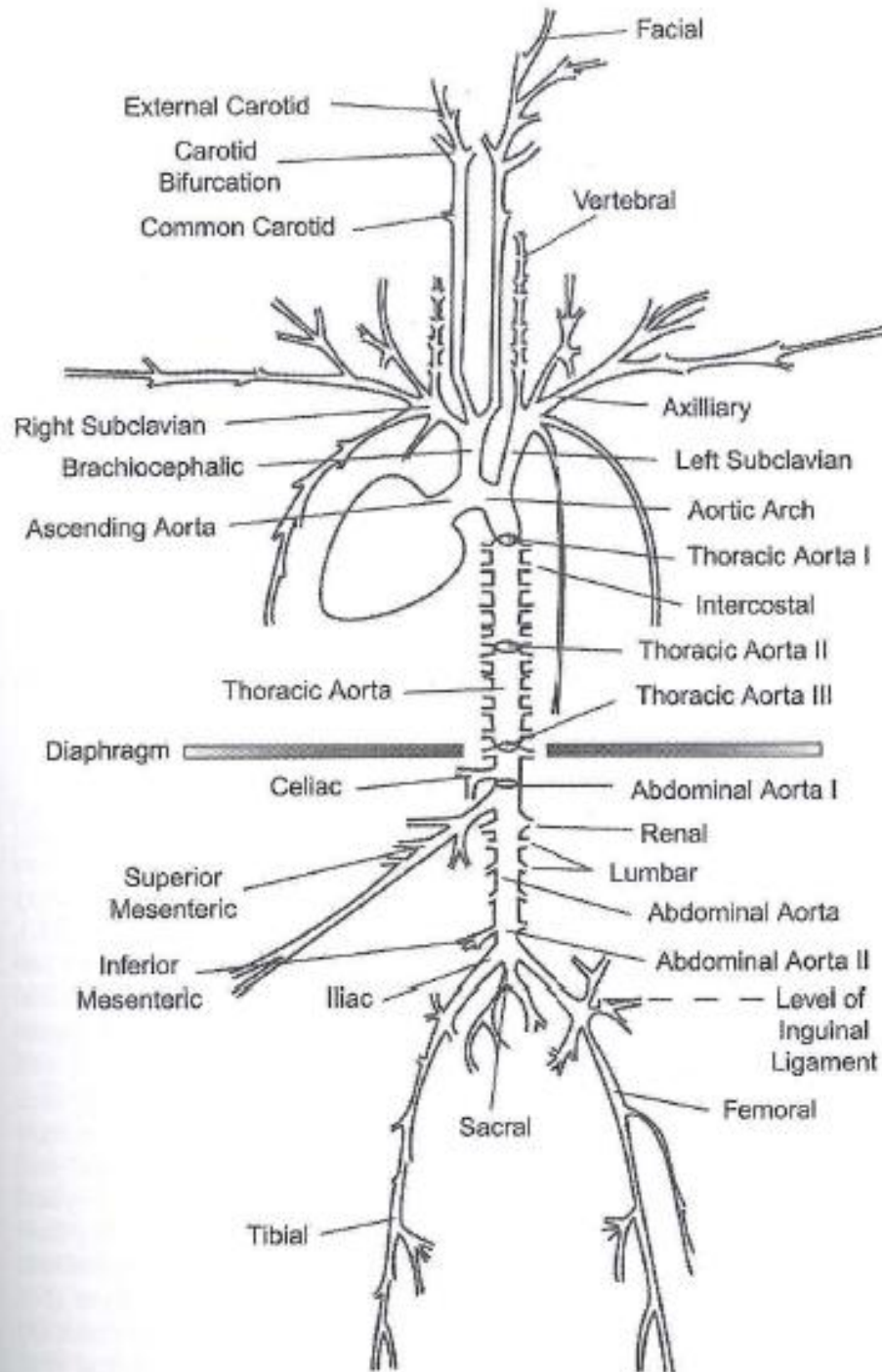
## Contents:

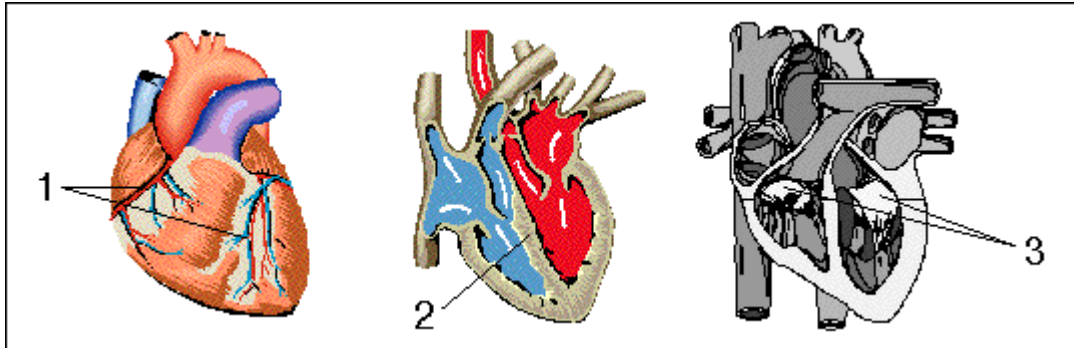
- Tissue biology basics. Link between microstructure and macroscale properties, and experimental characterization techniques. Structure, function and mechanical behaviour of tissues and organs (bone, cartilage, ligament, tendon, intervertebral disc, skin, nerve, skeletal muscle, heart, lung, artery, vein). Composition, function and mechanics of biological fluids.
- Cardiovascular biomechanics. Cardiovascular system. Biodynamic biological fluids. Biomechanics of the blood circulation. Ability to model specific problems such as the pulse wave in arteries, the effect of compression on the veins for the venous blood return
- Modeling approaches for continuum biomechanics of soft tissues: reminders of the basics in finite deformation mechanics and hyperelasticity, poroelasticity, chemoelasticity, other constitutive equations, relationships between the constitutive equations and the microstructure of tissues.
- Characterization of damage and failure mechanics of soft tissues, local analysis of rupture modes in soft tissues, experimental characterization and numerical implementation
- Advanced experimental approaches for soft tissue mechanics: full-field measurement techniques, imaging techniques, link between experiments and modeling
- Introduction to inverse problems, Identification of material parameters from full-field measurements, Characterization of maps of material parameters at different scales

# Blood circulation

Arteries and veins



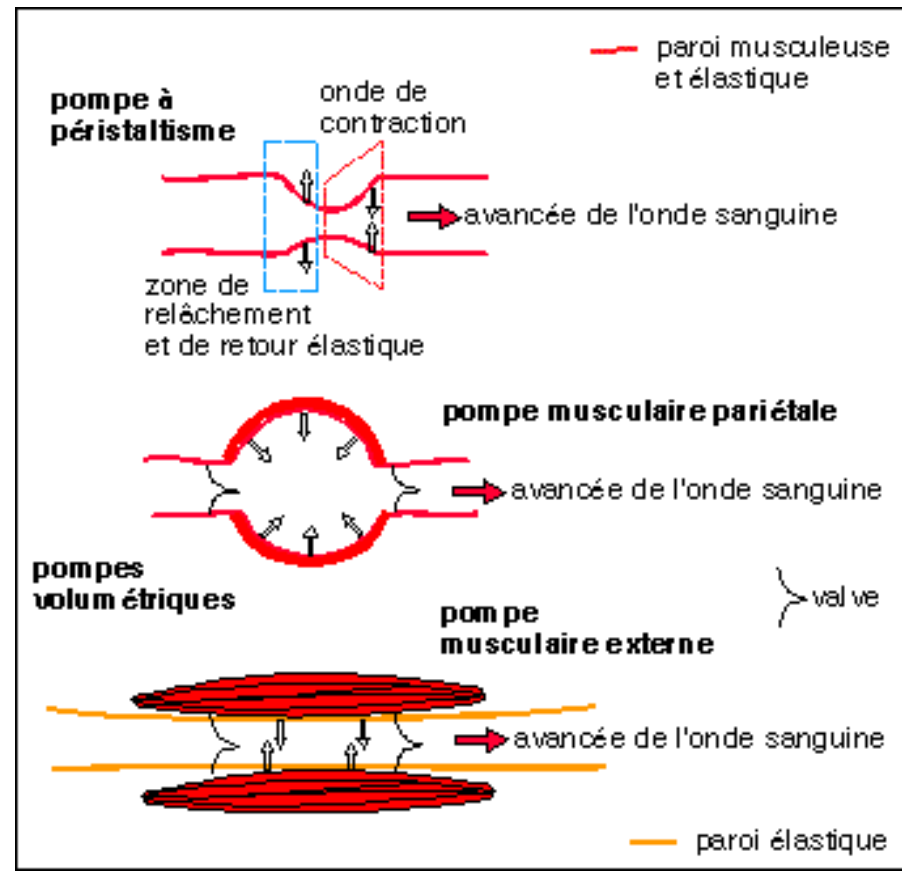




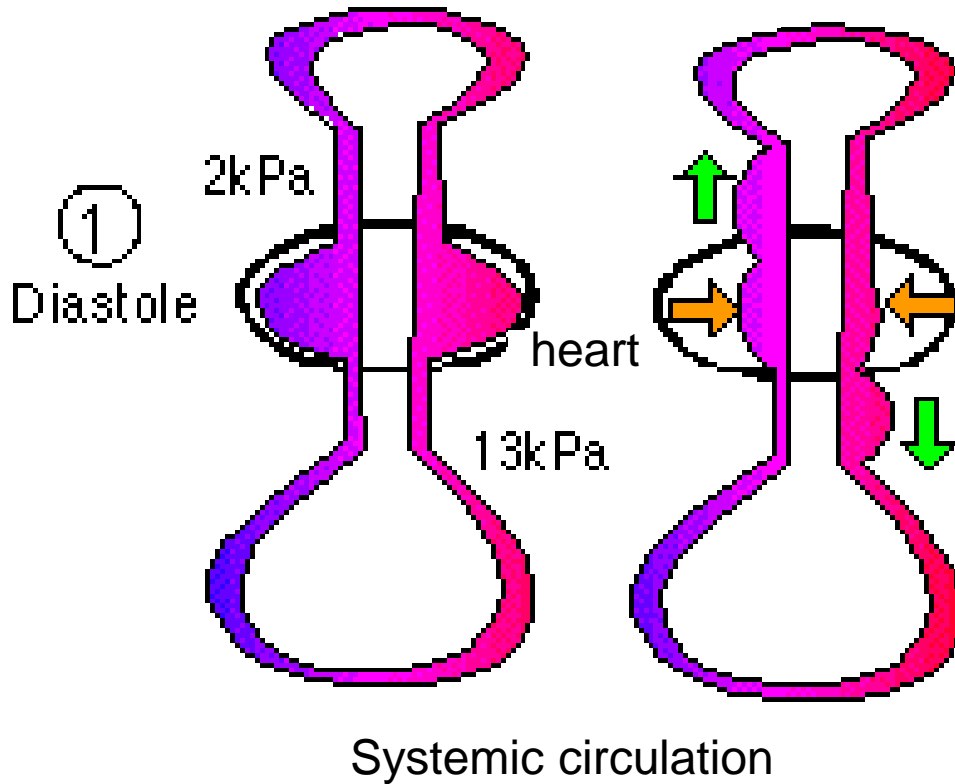
## Pomping = 2 states:

- Relaxed state (**diastole**), in which the heart is filled due to venous return,
- Contracted state (**systole**) or systolic ejection in which a certain volume of blood is projected into the aorta.

The cardiac pump is not the only pump in the circulatory system.



# Pulmonary circulation

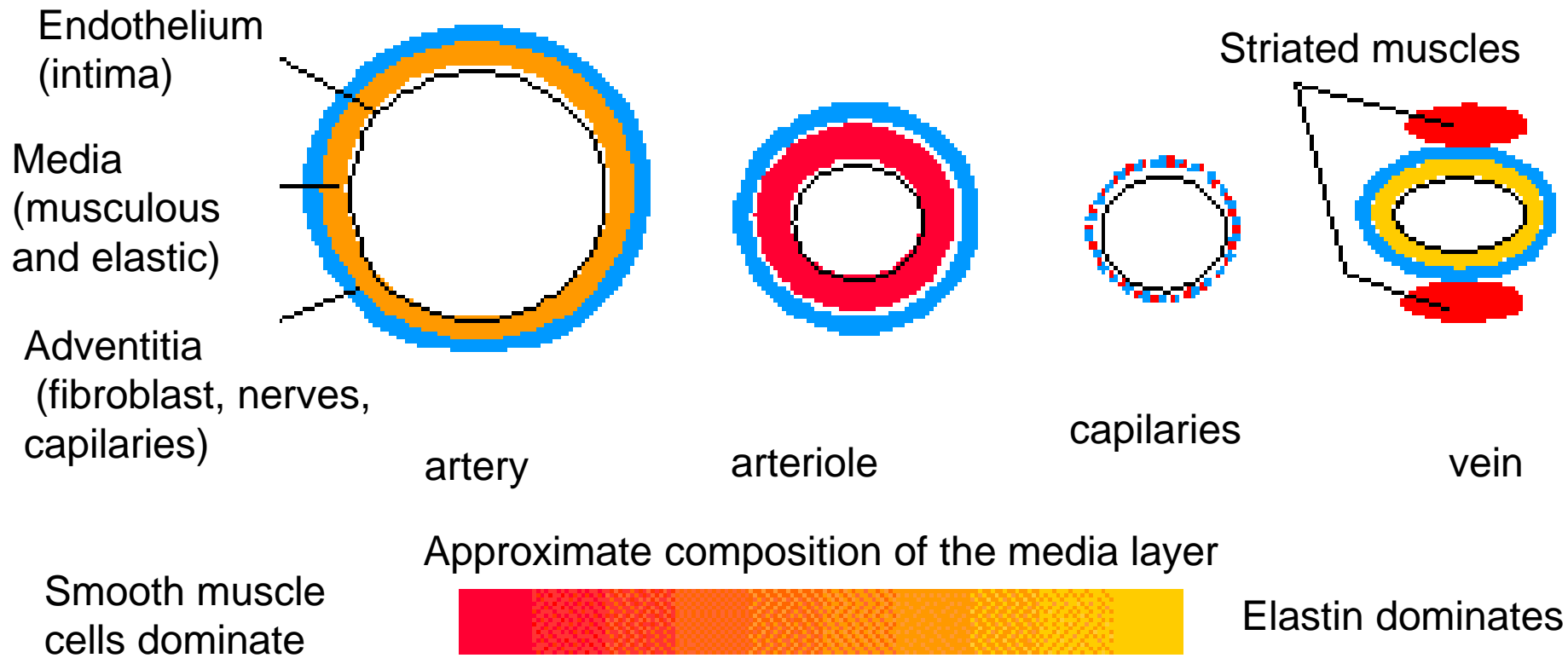


Elastic deformation of the pulmonary network: ejection from the right ventricle into the pulmonary artery

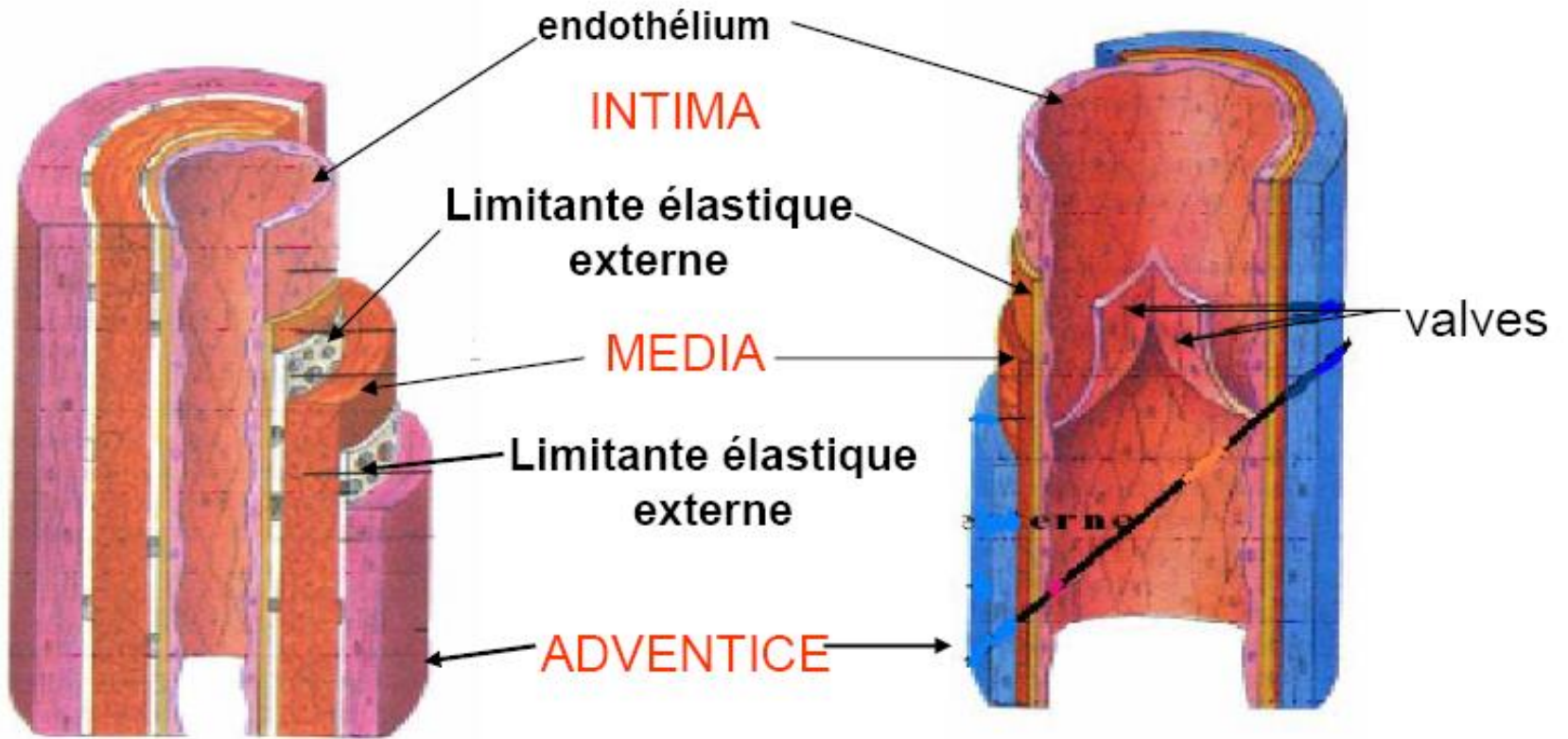
② Systole

Elastic deformation of the systemic network: ejection from the left ventricle into the aorta

Systemic circulation





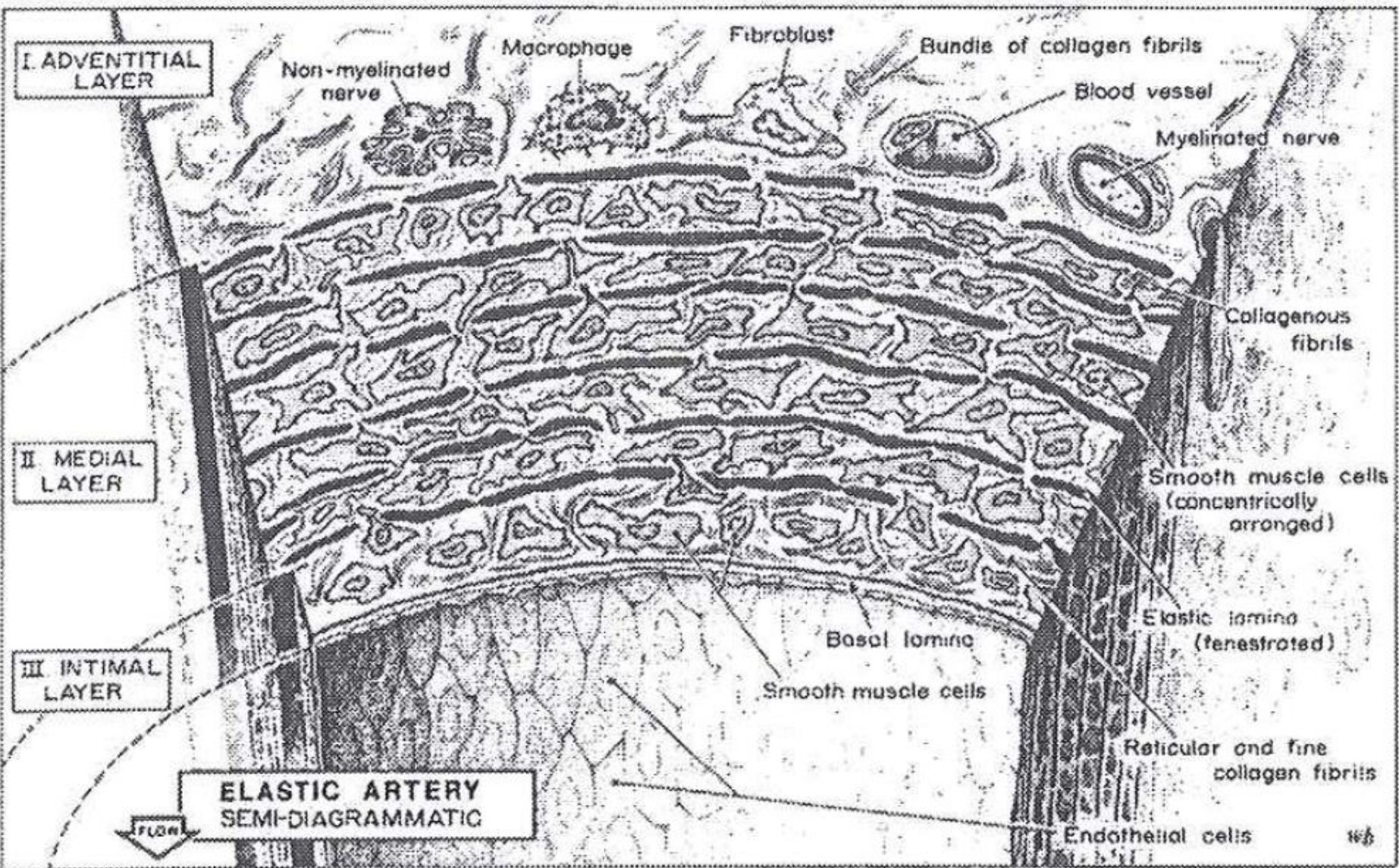


**ARTERE**

artery

**VEINE**

vein



I. ADVENTITIAL LAYER

II. MEDIAL LAYER

III. INTIMAL LAYER

ELASTIC ARTERY  
SEMI-DIAGRAMMATIC

Lumen

Non-myelinated nerve

Macrophage

Fibroblast

Bundie of collagen fibrils

Blood vessel

Myelinated nerve

Collagenous fibrils

Smooth muscle cells  
(concentrically arranged)

Elastic lamina  
(fenestrated)

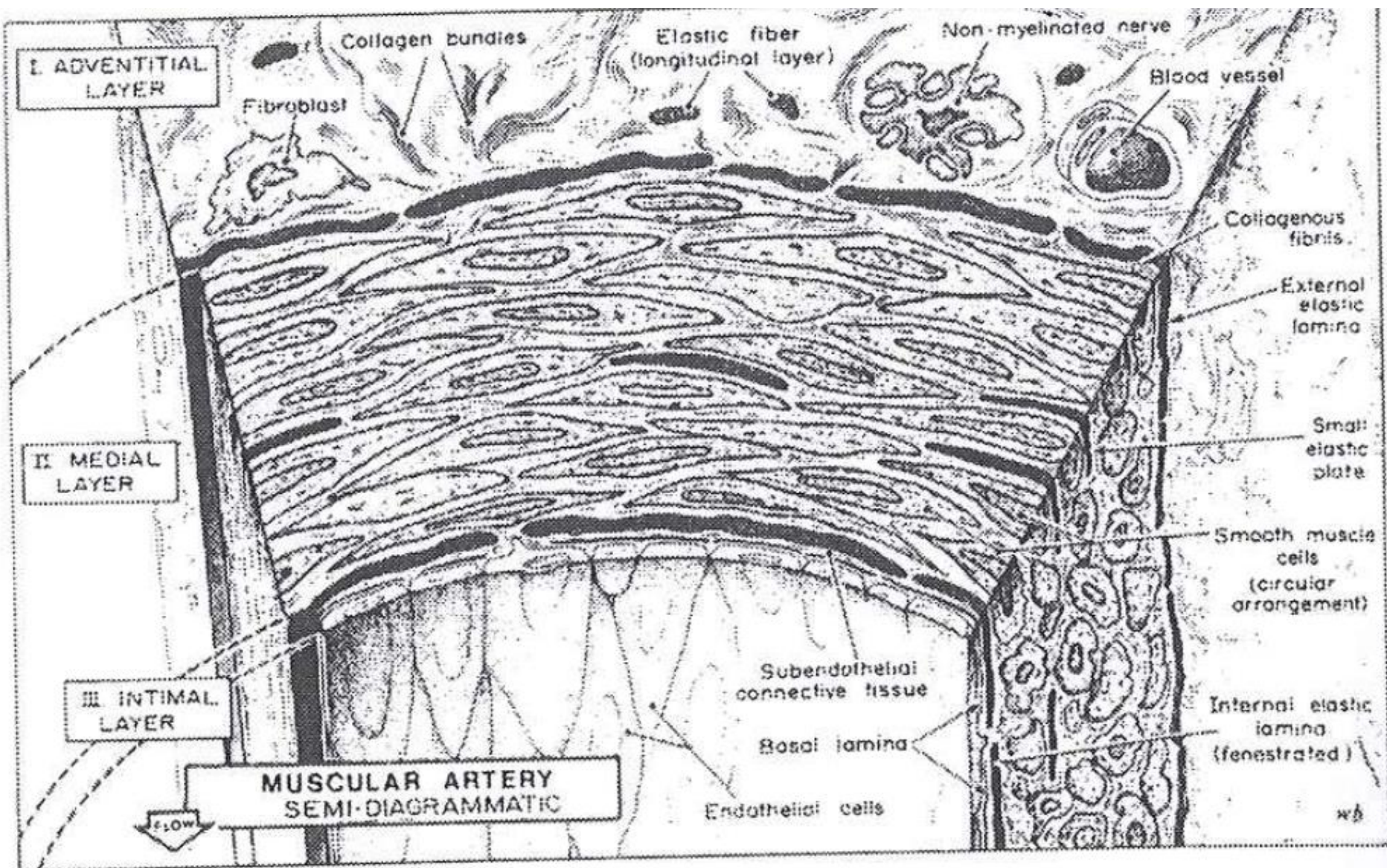
Basal lamina

Smooth muscle cells

Reticular and fine collagen fibrils

Endothelial cells

w/b

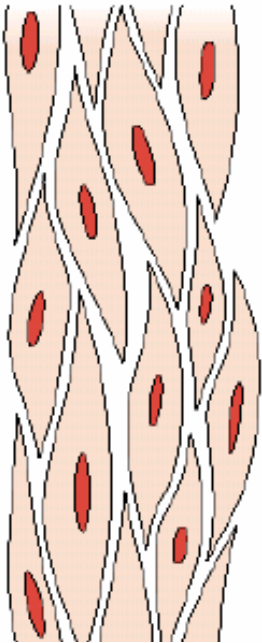


**MUSCULAR ARTERY  
SEMI-DIAGRAMMATIC**

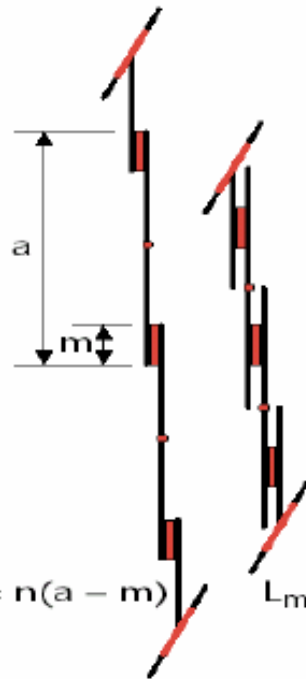
wb

# SMOOTH MUSCLE CELLS

fascicle



Single cell



$$L_{\max} = n(a - m)$$

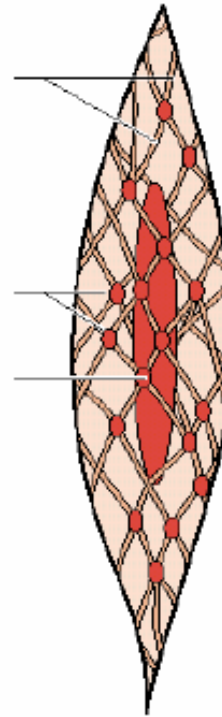
$$L_{\text{mid}} = na/2$$

(c)

100 Å  
filament  
bundles

Dense  
bodies

Nucleus

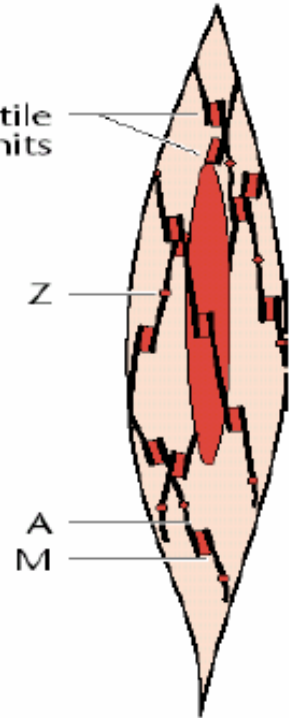


Contractile  
units

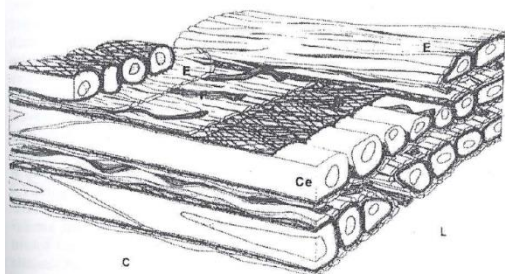
Z

A

M

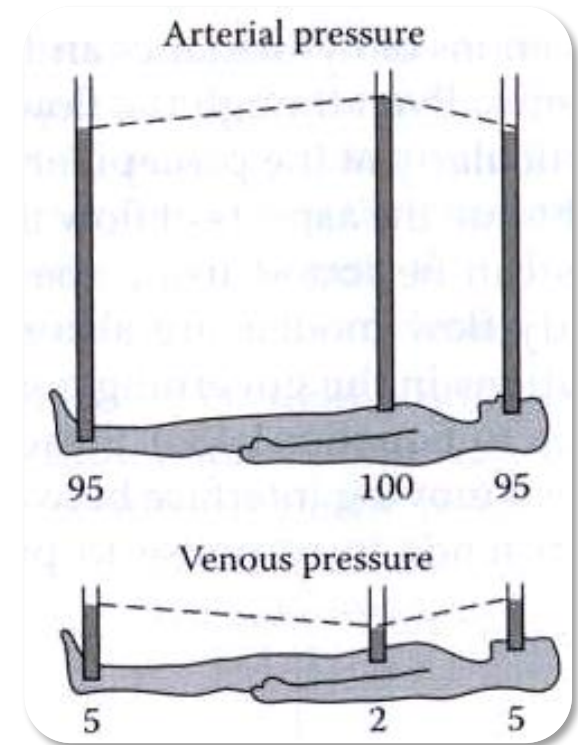


(d)



# Hydrostatics in the Circulation

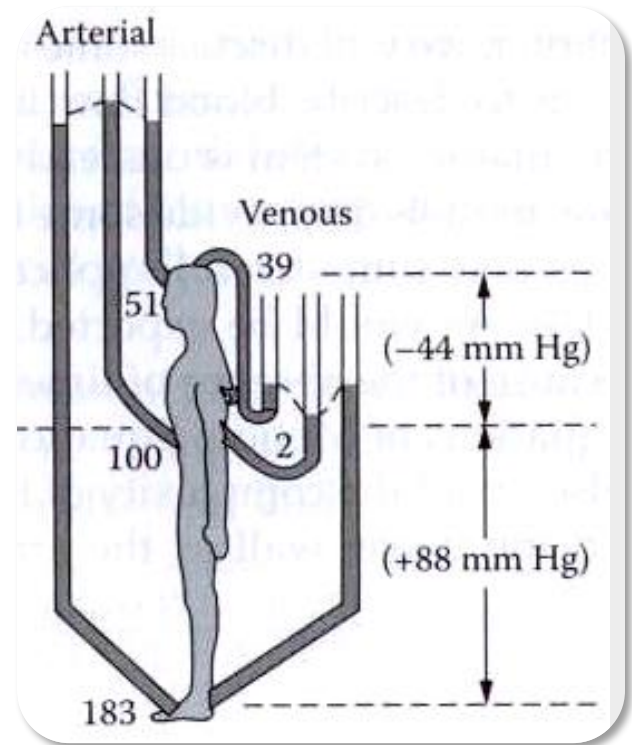
- Blood pressure in the “lying down” position
  - Arterial: 100 mmHg
  - Venous: 2 mmHg
- Distal pressure is lower



**Hydrostatic pressure differences in the circulation “lying down” position**

# Hydrostatics in the Circulation

- Blood pressure in the “standing up” position
  - Head artery: 50 mmHg
  - Leg artery: 180 mmHg
  - Head vein: -40 mmHg
  - Leg vein: 90 mmHg
- Pressure differences due to gravitational effects



**Hydrostatic pressure differences in the circulation “standing up” position**

# Hydrostatics in the Circulation

- Bernoulli equation:

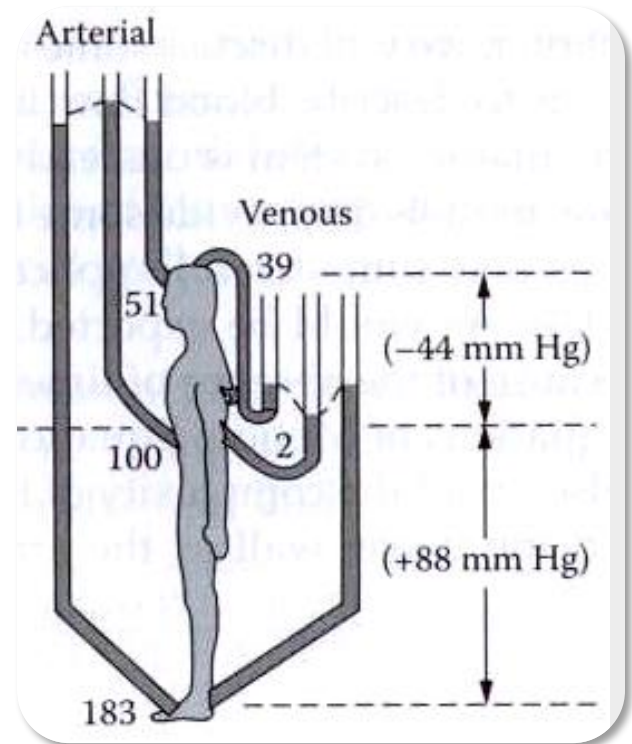
$$\frac{V^2}{2g} + \frac{p}{\rho g} + z = \text{const}$$

- Tube of constant cross section:

$$\Delta p = \rho g \Delta z$$

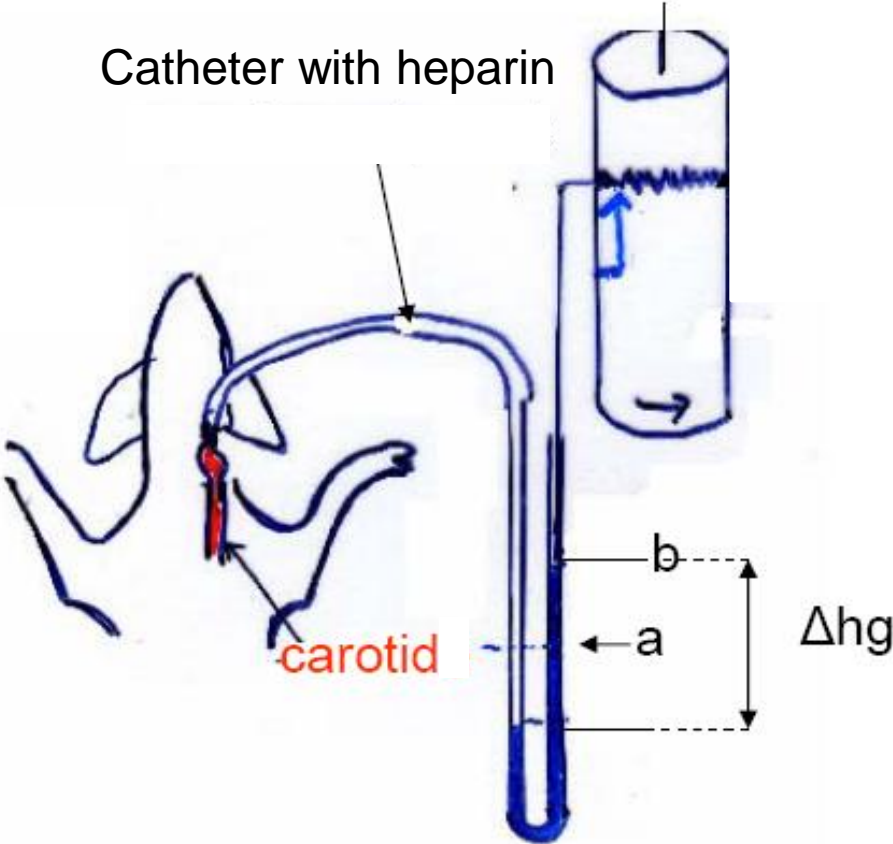
- Effects of pressure on vessels:

- Arteries are stiff: pressure does not affect volume
- Veins are distensible: pressure causes expansion



**Hydrostatic pressure differences in the circulation “standing up” position**

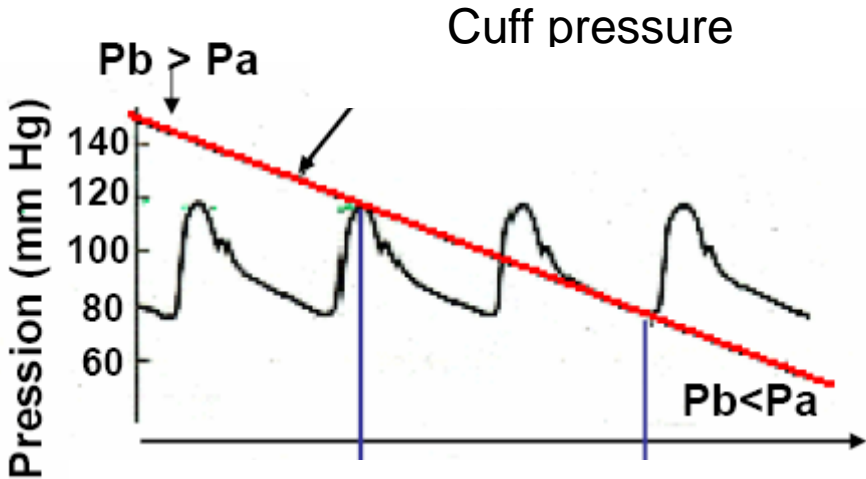
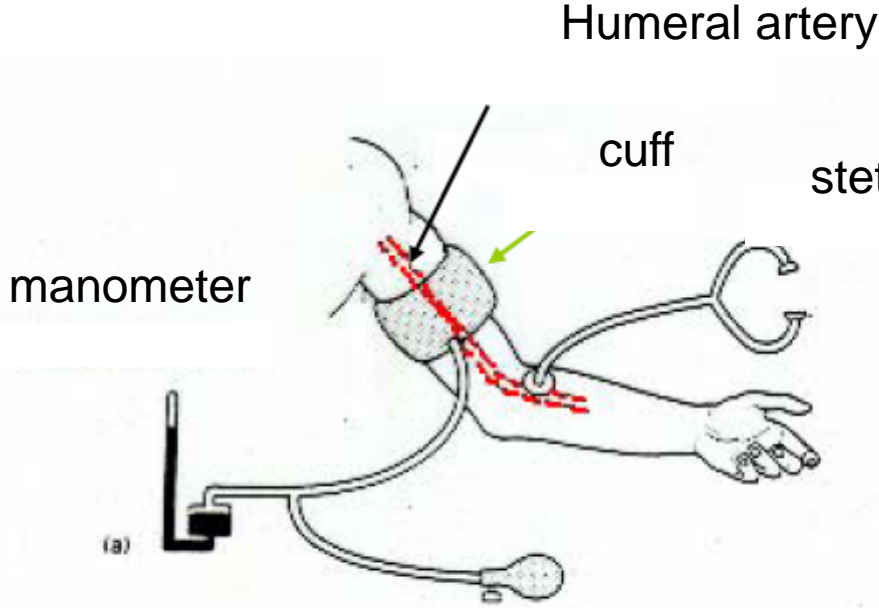
# DIRECT PRESSURE MEASUREMENT



Mercury manometer

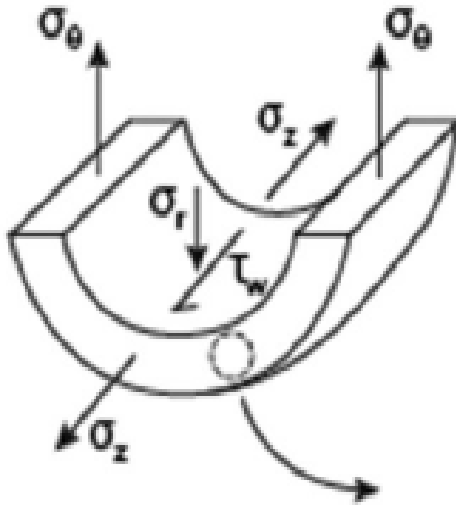


# CUFF MEASUREMENTS



Korotkoff noises

## Basic equations of arterial mechanics

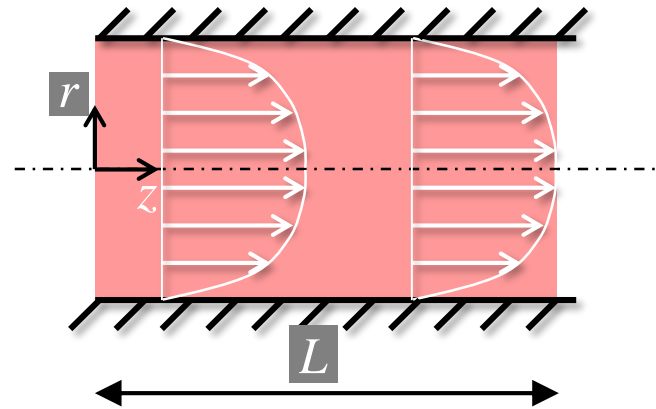


$$\tau_w = \frac{4\mu Q}{\pi a^3}, \quad \sigma_\theta = \frac{P a}{h}$$

# Hagen Poiseuille Model

- Assumptions:
  - incompressible
  - steady
  - laminar
  - circular cross section
- From exact analysis:

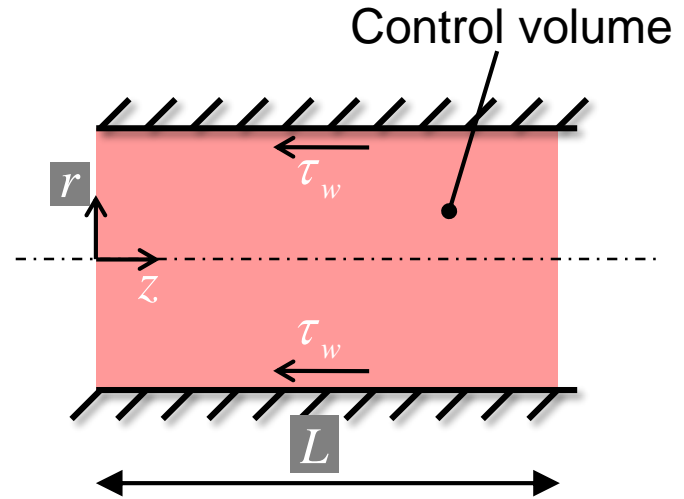
$$v_z(r) = \frac{\Delta p}{4\mu L} \left( r^2 - \frac{d^2}{4} \right)$$



$$Q = -\frac{\pi \Delta p d^4}{128\mu L}$$

# Hagen Poiseuille Model

- Assumptions:
  - incompressible
  - steady
  - laminar
  - circular cross section



- From control volume analysis:

$$\Delta p = - \frac{4\tau_w L}{d}$$

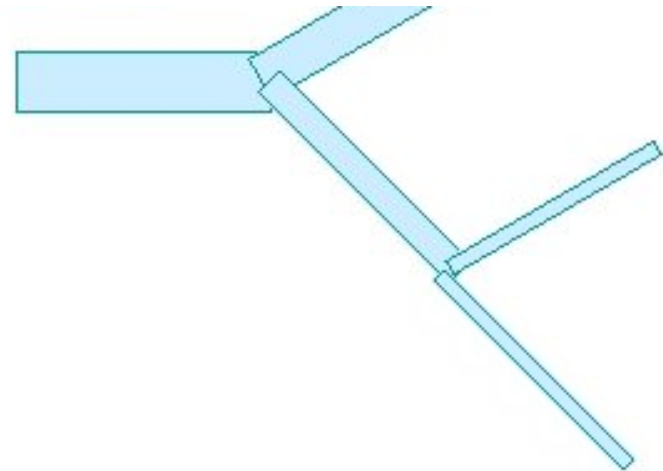
# Murray's law

- Blood Flow in vessels
- Minimization of 'work'
- Murray's Law:

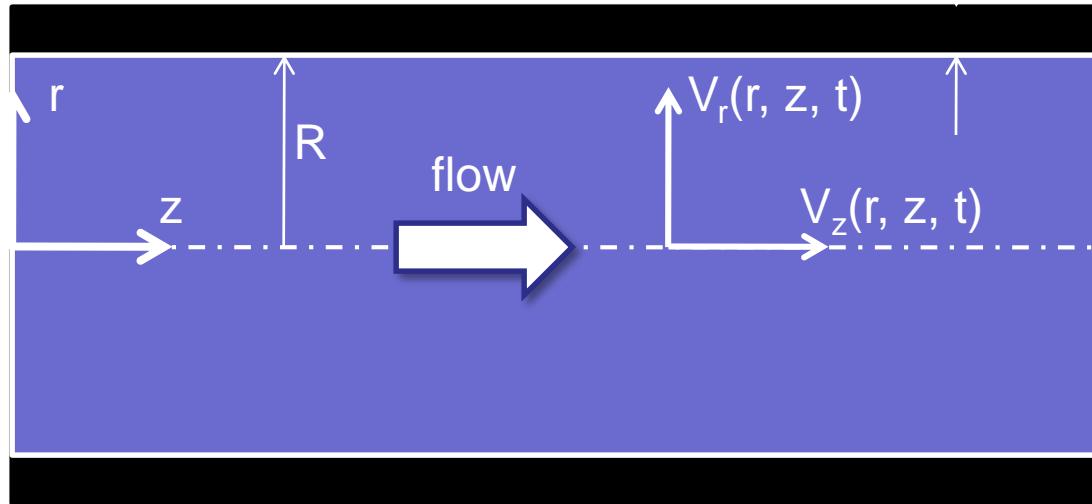
$$\sum r_{in}^3 = \sum r_{out}^3$$

- Laminar Flow, negligible friction loss (other than that due to viscous loss in laminar flow), steady
- Turbulent, pulsating flow
- Assume

$$\Delta p = \frac{8\mu L Q}{\pi R^4} \quad \text{Work} = Q \Delta p = \alpha \frac{Q^2}{r^4}$$



# Moens Korteweg equation

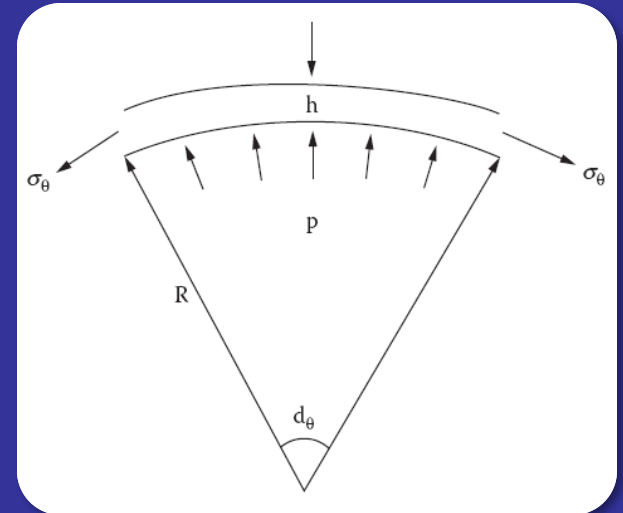


**Infinitely long, thin-walled elastic tube of circular cross-section**

# Moens-Korteweg equation

- Tube equation of motion:

$$\rho_t h R d\theta \frac{d^2 \eta}{dt^2} = R p d\theta - \sigma_\theta h d\theta$$



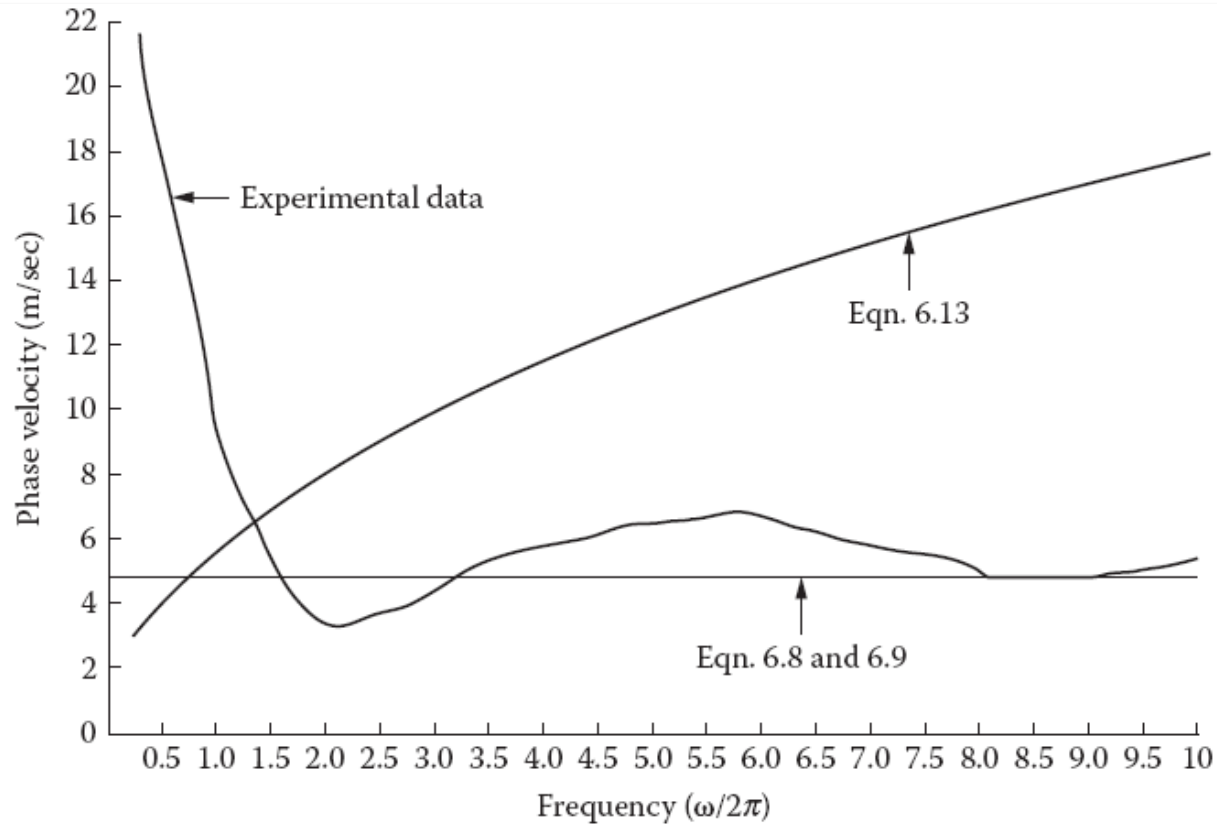
- Coupling with fluid motion (with inertial effects):

$$\frac{\partial^2 p}{\partial z^2} = \frac{1}{c_0^2} \frac{\partial^2 p}{\partial t^2}$$

where

$$c_0^2(\omega) = \frac{hE}{2\rho R} \left( 1 - \frac{\omega^2 \rho_t R^2}{E} \right)$$

# Experimental vs. Theoretical $c_0$



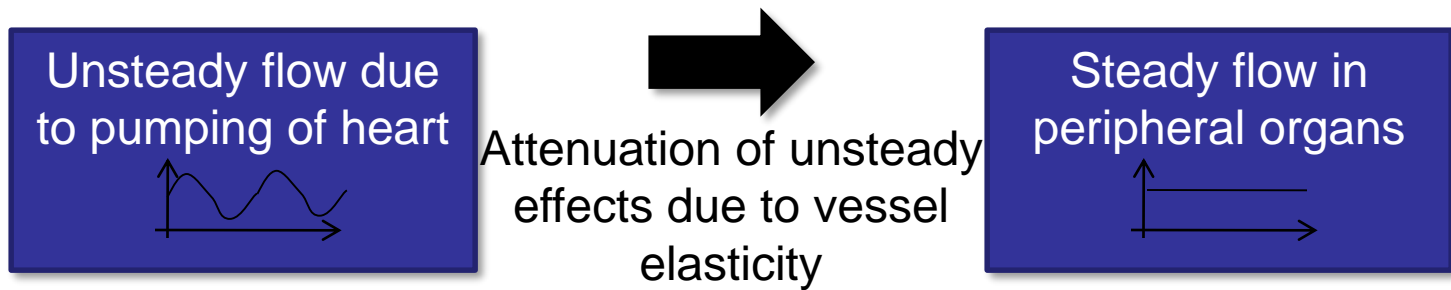
**FIGURE 6.5**

Pulse wave velocity plotted as a function of frequency from the theoretical models compared with experimental data. (Experimental curve redrawn from Noordergraaf, (1978) Elsevier, Philadelphia. With permission.)



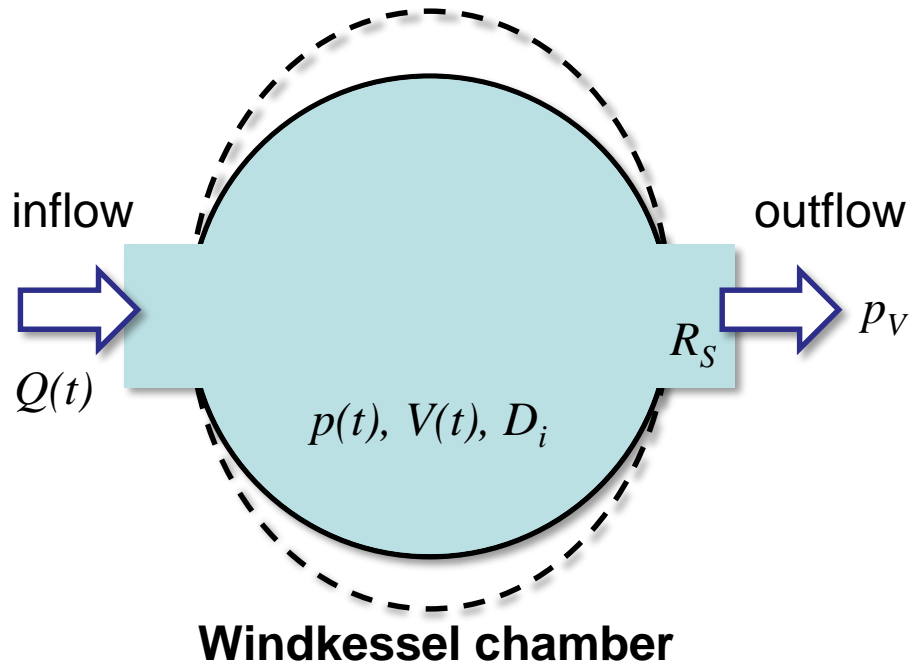
# Windkessel Theory

- Simplified model
- Arterial system modeled as elastic storage vessels



- Arteries = interconnected tubes with storage capacity

# Windkessel Theory



Variable	Definition
$s$	
$p$	Windkessel chamber pressure
$V$	Windkessel chamber volume
$D_i$	Chamber distensibility
$R_s$	Peripheral resistance
$Q$	Ventricular ejection flow rate
$p_v$	Venous pressure

## Definitions:

- Inflow: fluid pumped intermittently by ventricular ejection
- Outflow: calculated based on Poiseuille theory

# Windkessel Solution

- Pressure pulse solution

- Systole ( $0 < t < t_s$ ):

$$p(t) = R_S Q_0 - (R_S Q_0 - p_0) e^{-\frac{t}{R_S D_i}}$$

- Diastole ( $t_s < t < T$ ):

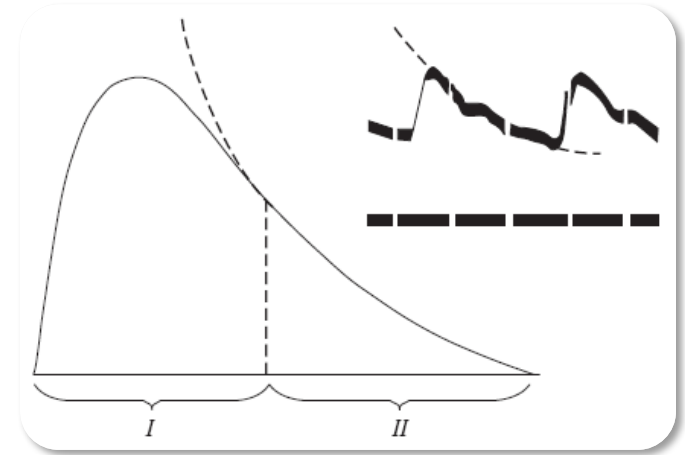
$$p(t) = p_T e^{\frac{T-t}{R_S D_i}}$$

$p_0$ : pressure at  $t=0$

$p_T$ : pressure at  $t=T$

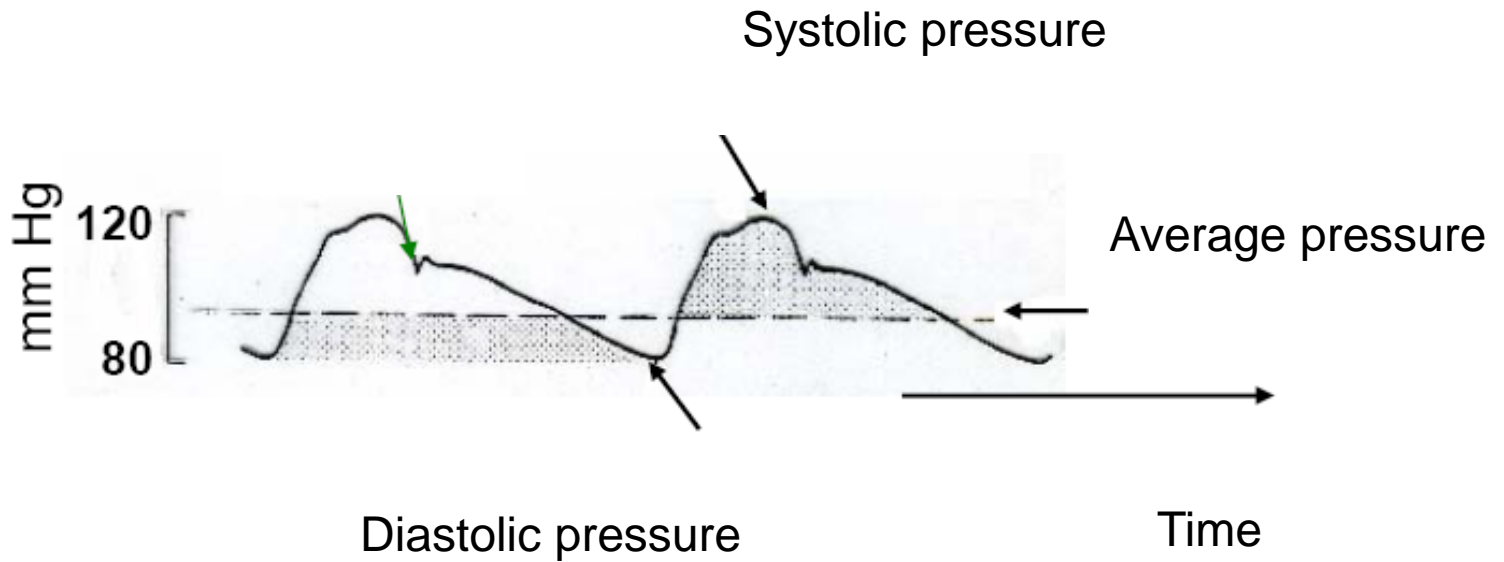
- Stroke volume

$$V_S = \int_0^{t_s} Q(t) dt = Q_0 t_s$$



Windkessel (left) vs. actual (right) pressure pulse

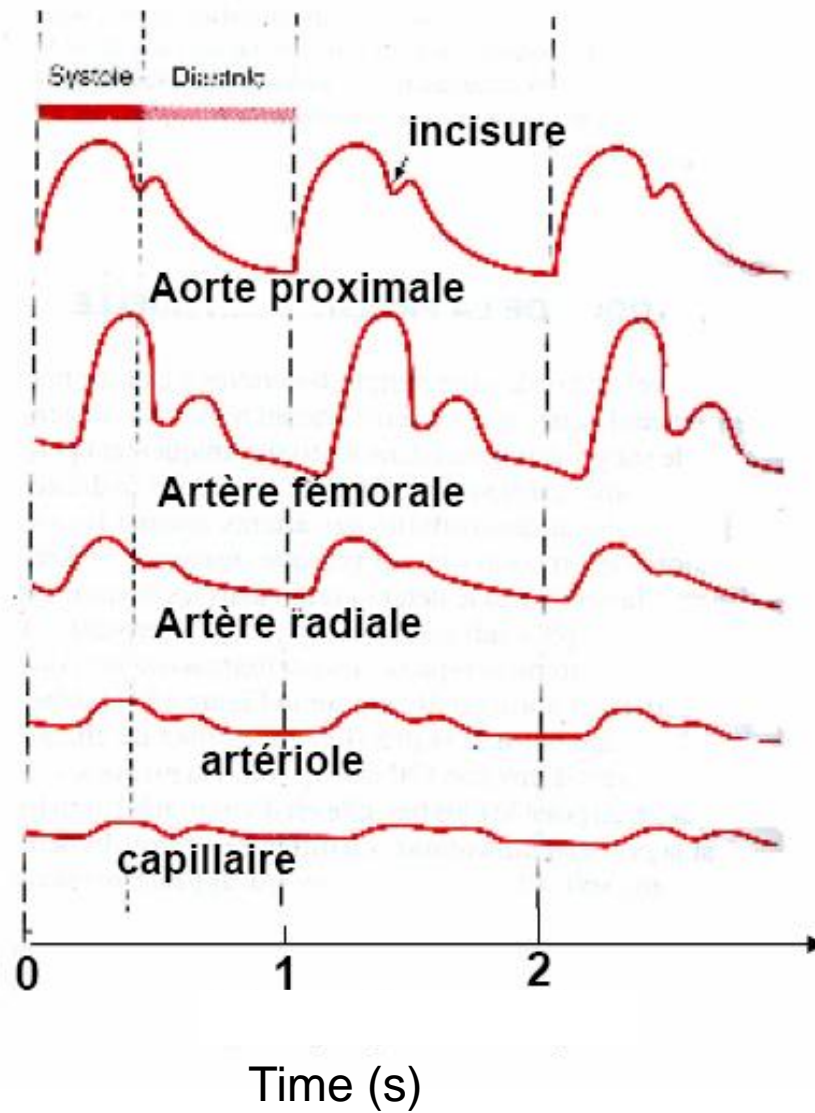
# PULSE PRESSURE



In the human, in average, the arterial pressure measured at the forearm is at 40 years:  
Diastolic: 80mmHg, systolic: 140mmHg.

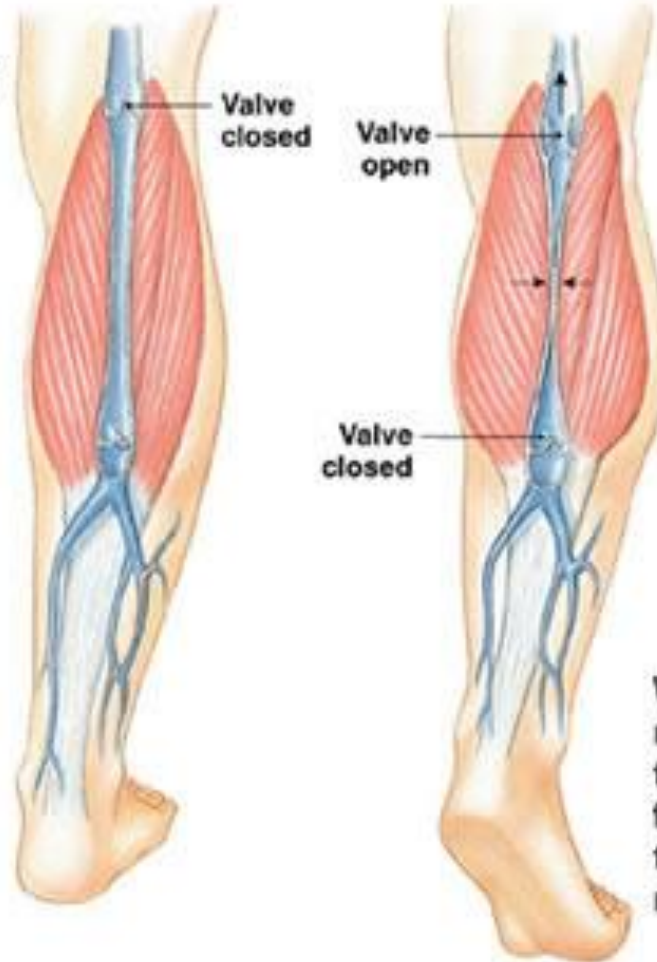
According to WHO, pathologic pressure is defined ... (arterial hypertension)

# Evolution of pressure oscillations throughout the vascular tree



# Vein biomechanics

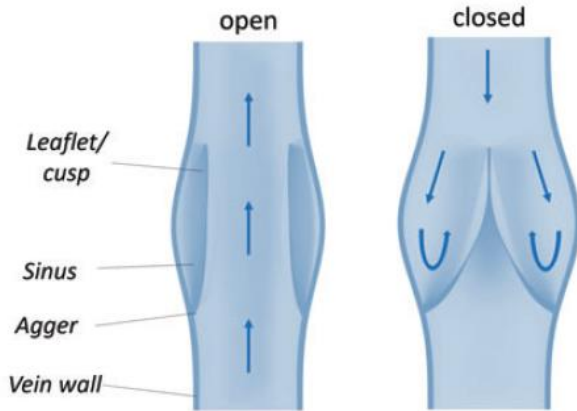
Valves in the veins prevent backflow of blood.



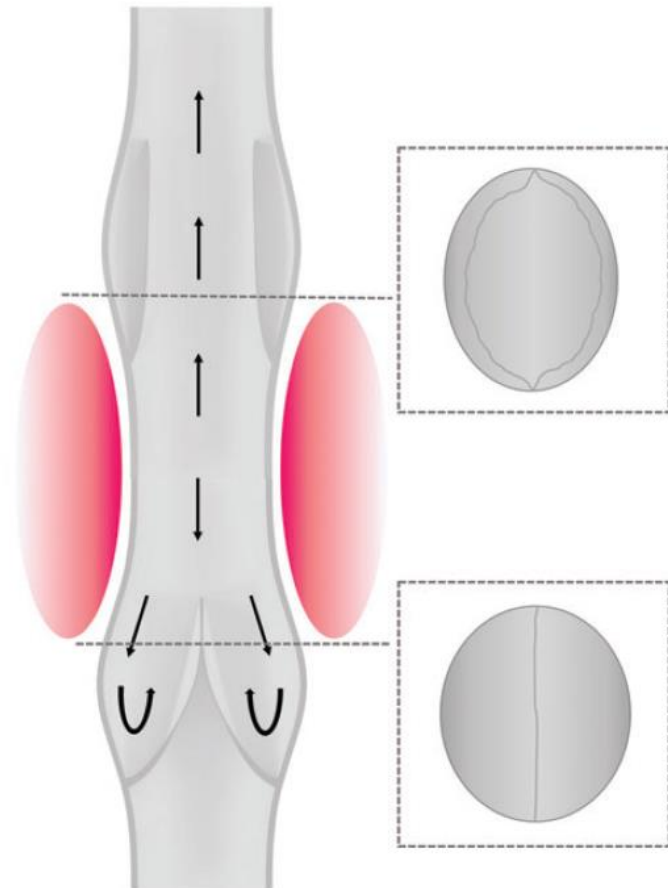
When the skeletal muscles compress the veins, they force blood toward the heart (the skeletal muscle pump).

# Vein biomechanics

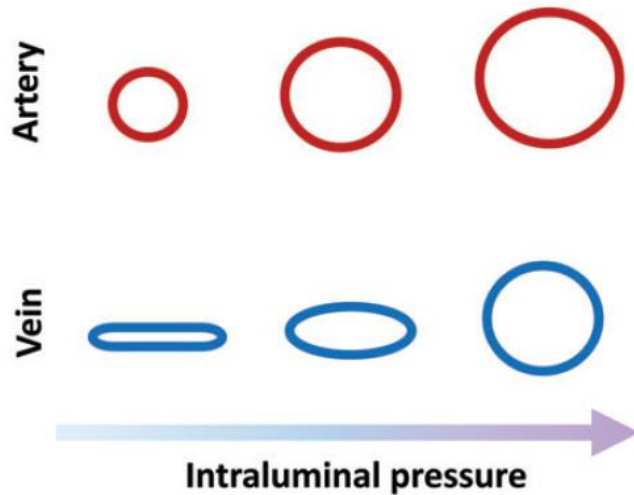
**a** Bicuspid human venous valve



**c** Calf contraction and venous valve disposition



**b** Cross section of artery and vein under increasing pressure



# PROBLEM OF VEIN BIOMECHANICS

Considering the pressure distribution due to gravity and the mechanical behaviour of veins shown in the figure below, explain why we can feel dizzy when we stand up quickly from squatting or crouching.

